

# Manipulation of ultracold atoms using magnetic and optical fields

Matthew J. Pritchard

---

A thesis submitted in partial fulfilment  
of the requirements for the degree of  
Doctor of Philosophy



Department of Physics  
University of Durham

September 2006

# Manipulation of ultracold atoms using magnetic and optical fields

Matthew J. Pritchard

---

## Abstract

The loading and guiding of a launched cloud of cold atoms with the optical dipole force are theoretically and numerically modelled. A far-off resonance trap can be realised using a high power Gaussian mode laser, red-detuned with respect to the principal atomic resonance (Rb 5s-5p). The optimum strategy for loading typically 30% of the atoms from a Magneto optical trap and guiding them vertically through 22 cm is discussed. During the transport the radial size of the cloud is confined to a few hundred microns, whereas the unconfined axial size grows to be approximately 1 cm. It is proposed that the cloud can be focused in three dimensions at the apex of the motion by using a single magnetic impulse to achieve axial focusing.

A theoretical study of six current-carrying coil and bar arrangements that generate magnetic lenses is made. An investigation of focusing aberrations show that, for typical experimental parameters, the widely used assumption of a purely harmonic lens is often inaccurate. A new focusing regime is discussed: isotropic 3D focusing of atoms with a single magnetic lens. The baseball lens offers the best possibility for isotropically focusing a cloud of weak-field-seeking atoms in 3D.

A pair of magnetic lens pulses can also be used to create a 3D focus (the alternate-gradient method). The two possible pulse sequences are discussed and it is found that they are ideal for loading both ‘pancake’ and ‘sausage’ shaped magnetic/optical microtraps. It is shown that focusing aberrations are considerably smaller for double-impulse magnetic lenses compared to single-impulse magnetic lenses.

The thesis concludes by describing the steps taken towards creating a 3D quasi-electrostatic lattice for  $^{85}\text{Rb}$ , using a  $\text{CO}_2$  laser. The resulting lattice of trapped atoms will have a low decoherence, and with resolvable lattice sites, it therefore provides a useful system to implement quantum information processing.

# Declaration

I confirm that no part of the material offered has previously been submitted by myself for a degree in this or any other University. Where material has been generated through joint work, the work of others has been indicated.

Matthew J. Pritchard  
Durham, 21<sup>st</sup> September 2006

The copyright of this thesis rests with the author. No quotation from it should be published without their prior written consent and information derived from it should be acknowledged.

# Acknowledgements

I'm very grateful to my joint supervisors Charles Adams and Ifan Hughes. Their passion for physics has been an inspiration. Their wealth of knowledge has been invaluable.

The majority of what I have learnt these past years has been through the interaction with other AtMol group members. Thanks to the three Simons, Robert, Nick and Griff for answering many questions. To Dave and Graham, your assistance was appreciated, your friendship highly valued. Special thanks to Kev, lab partner and the person who bore the brunt of my eccentricities on a daily basis. I hope you can iron out all the creases I put in the experiment and make some nice physics.

I'd also like to thank the physics department's technical support groups for their expertise they've shared with me over the years. Thanks to the personnel in: Audio Visual, Electronics, Engineering, Finance, UG teaching labs and Computing. Away from Durham, links with Strathclyde University have been fruitful. Aidan Arnold has been a constant source of new ideas and Mathematica fixes. Erling Riis and Robert Wiley have helped with the vacuum chamber design and construction.

Outside the world of physics (yes, it does exist!) I have enjoyed the friendship, support, guidance and fellowship from numerous people. Thanks to Mildert MCR for making me feel normal, Durham Improv for making me laugh and Kings Church massif for making it together. To my parents, your love and belief these last 25 years has been immense. And finally...thanks God.

*“The fear of the LORD is the beginning of knowledge, but fools despise wisdom and discipline.”*

Proverbs 1v7

# Contents

<b>Abstract</b>	<b>i</b>
<b>Declaration</b>	<b>ii</b>
<b>Acknowledgements</b>	<b>iii</b>
<b>Table of contents</b>	<b>vii</b>
<b>List of figures</b>	<b>x</b>
<b>List of tables</b>	<b>xi</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Atom optics . . . . .	2
1.1.1 Matter interactions . . . . .	2
1.1.2 Electric field interactions . . . . .	2
1.1.3 Magnetic field interactions . . . . .	3
1.1.4 Light field interactions . . . . .	4
1.2 Research aims and outline . . . . .	7
1.2.1 Atom guiding and focusing . . . . .	7
1.2.2 Enhanced loading of optical lattices . . . . .	8
1.3 Thesis structure . . . . .	9
1.4 Publications . . . . .	11
<b>2 Background theory: Atoms and light</b>	<b>12</b>
2.1 Optical forces . . . . .	12
2.1.1 Two-level model . . . . .	13
2.2 Laser cooling and the scattering force . . . . .	15
2.2.1 The Magneto-optical trap . . . . .	18
2.2.2 Implementing laser cooling in $^{85}\text{Rb}$ . . . . .	19
2.3 Laser trapping and the dipole force . . . . .	20
2.3.1 Polarisability . . . . .	20
<b>3 Laser guiding</b>	<b>26</b>
3.1 Gaussian laser beam profile . . . . .	26
3.2 Laser guide modelling . . . . .	27

3.2.1	The dipole force . . . . .	29
3.2.2	Computer simulation . . . . .	30
3.3	Loading the guide . . . . .	31
3.4	Transport losses . . . . .	33
3.4.1	Truncation losses . . . . .	33
3.4.2	Diffraction losses . . . . .	34
<b>4</b>	<b>Magnetic lens design</b>	<b>38</b>
4.1	The Stern-Gerlach force . . . . .	38
4.2	The principle of magnetic lenses . . . . .	39
4.3	Magnetic fields from current bars and circular coils . . . . .	41
4.4	Configurations for realising magnetic lenses . . . . .	44
4.4.1	Strategy I: a single coil . . . . .	44
4.4.2	Strategies II and III: a pair of axially-displaced coils ( $I_1 = I_2$ ) . . . . .	44
4.4.3	Strategy IV: a pair of axially-displaced coils ( $I_1 \neq I_2$ ) . . . . .	47
4.4.4	Strategy V: an axially offset single coil . . . . .	48
4.4.5	Strategy VI: Ioffe-Pritchard configuration . . . . .	48
4.5	The harmonicity of the magnetic lenses . . . . .	51
4.6	Alternate-gradient focusing . . . . .	52
<b>5</b>	<b>Time sequences for pulsed magnetic focusing</b>	<b>54</b>
5.1	$ABCD$ matrices . . . . .	54
5.1.1	Thick and thin lenses . . . . .	56
5.2	Single-impulse focusing . . . . .	57
5.2.1	Lenses with a constant $\mathbf{a}_0$ term . . . . .	58
5.3	Double-impulse focusing . . . . .	61
<b>6</b>	<b>Results: Pulsed magnetic focusing</b>	<b>65</b>
6.1	Methodology . . . . .	65
6.1.1	Root mean square cloud radius . . . . .	66
6.1.2	Atoms in the harmonic region . . . . .	66
6.2	Single-impulse magnetic focusing . . . . .	68
6.2.1	Strategy I: axial defocusing/radial focusing . . . . .	68
6.2.2	Strategies II-III: axial/radial focusing . . . . .	70
6.2.3	Strategies IV-VI: isotropic 3D focusing . . . . .	72
6.3	Magnetic focusing and laser guiding . . . . .	74
6.3.1	Strategy IV: axial-only focusing . . . . .	75
6.3.2	Strategies II-III: axial/radial focusing . . . . .	76
6.3.3	Transported cloud properties . . . . .	79
6.4	Double-impulse magnetic focusing . . . . .	81
6.4.1	Transported cloud properties . . . . .	82

---

<b>7</b>	<b>Optical lattices and experiment design</b>	<b>87</b>
7.1	Optical lattices . . . . .	88
7.1.1	Single-site addressability . . . . .	91
7.2	Experiment: design criteria . . . . .	92
<b>8</b>	<b>Experiment construction</b>	<b>93</b>
8.1	Vacuum chamber and magnetic fields . . . . .	94
8.1.1	The pyramid MOT . . . . .	95
8.1.2	The science chamber . . . . .	99
8.1.3	Construction, pumping and testing . . . . .	101
8.2	Diode lasers and optics for cooling . . . . .	102
8.2.1	External cavity diode lasers . . . . .	102
8.2.2	Laser spectroscopy and frequency locking . . . . .	105
8.2.3	Implementing laser cooling . . . . .	113
8.2.4	Low cost laser shutters . . . . .	116
8.3	CO <sub>2</sub> laser and dipole trapping optics . . . . .	120
8.4	Imaging and computer control . . . . .	121
<b>9</b>	<b>Optimising the MOTs</b>	<b>125</b>
9.1	P-MOT . . . . .	125
9.2	S-MOT . . . . .	127
9.2.1	Fluorescence and atom number . . . . .	127
9.2.2	Loading curves and optimisation . . . . .	129
<b>10</b>	<b>Discussion and conclusions</b>	<b>134</b>
10.1	Pulsed magnetic focusing . . . . .	134
10.1.1	Future work . . . . .	136
10.2	3D quasi-electrostatic lattices . . . . .	137
10.2.1	Future work . . . . .	137
<b>A</b>	<b>Abbreviations used</b>	<b>138</b>
<b>B</b>	<b>Symbol definitions</b>	<b>139</b>
<b>C</b>	<b>Values and constants</b>	<b>142</b>
<b>D</b>	<b>Atomic structure of Rb</b>	<b>143</b>
<b>E</b>	<b>Collision rate</b>	<b>144</b>
<b>F</b>	<b>Mathematica computer code</b>	<b>145</b>
<b>G</b>	<b>Fibre optic alignment</b>	<b>147</b>
<b>H</b>	<b>Knife edge measurements</b>	<b>149</b>



# List of Figures

1.1	Thesis structure. . . . .	10
2.1	Two-level atomic model. . . . .	14
2.2	Radiation pressure. . . . .	16
2.3	Doppler force vs. velocity. . . . .	17
2.4	MOT operation and design. . . . .	18
2.5	$^{85}\text{Rb}$ cooling transitions. . . . .	19
2.6	$Q$ -matrix structure. . . . .	22
2.7	Differential light-shifts. . . . .	25
3.1	Gaussian laser beam profile. . . . .	27
3.2	Model setup for laser guiding and magnetic focusing. . . . .	28
3.3	Rayleigh length and $1/e^2$ radius vs. beam waist. . . . .	29
3.4	Radial and axial acceleration vs. distance. . . . .	30
3.5	Loading efficiency plotted for varying beam waist and $z$ focal point. . . . .	32
3.6	Aperture transmission vs. aperture height and aperture radius. . . . .	34
3.7	The overall transport efficiency of the laser guide. . . . .	35
3.8	Phase-space plots of laser guiding. . . . .	37
4.1	Breit-Rabi diagram for $^{85}\text{Rb}$ . . . . .	39
4.2	B-field magnitude for a single coil. . . . .	42
4.3	The six lens strategies for pulsed magnetic focusing. . . . .	45
4.4	The B-field magnitudes for each of the six strategies. . . . .	46
4.5	The curvature of a coil pair vs. separation. . . . .	47
4.6	The departure from harmonicity for the six lens designs. . . . .	52
4.7	The principle of alternate-gradient focusing. . . . .	53
5.1	Timing sequence for a single-impulse lens system. . . . .	57
5.2	$\lambda$ vs. pulse duration. . . . .	59
5.3	Vertical centre of mass position vs. time. . . . .	60
5.4	Timing sequence for a double-impulse lens system. . . . .	61
5.5	Analytical solutions to double-impulse focusing. . . . .	64
6.1	Renormalisation of the cloud's dimensions. . . . .	67
6.2	The trajectories of 25 atoms subject to a Strategy I lens. . . . .	68
6.3	A shell plot of atoms passing through a Strategy I lens. . . . .	69

6.4	Change in cloud size vs. coil radius. . . . .	70
6.5	Comparison between Strategy I and II lenses. . . . .	71
6.6	Simulation of atoms sent through an isotropic Strategy IV lens. . . . .	73
6.7	The effect of the non-Gaussian wings in the distribution. . . . .	73
6.8	The potential energy surface of the laser and axial-only lens. . . . .	75
6.9	$\sigma_z/\sigma_{z_i}$ vs. time for axial-only lenses. . . . .	76
6.10	The potential energy surface of the laser and a Strategy III lens. . . . .	77
6.11	The trajectories of atoms passing along the laser guide. . . . .	77
6.12	Losses from the laser guide due to magnetic focusing. . . . .	78
6.13	Focus quality of the combined laser guide and magnetic lens. . . . .	79
6.14	The relative density increase for alternate-gradient lensing. . . . .	82
6.15	Phase-space plots of the AR and RA strategies. . . . .	83
7.1	1D optical lattice potential surface. . . . .	88
7.2	The 4 beam geometry used to create the 3D lattice. . . . .	89
7.3	1D slice through the face-centred cubic lattice. . . . .	90
7.4	2D slice through the face-centred cubic lattice. . . . .	90
7.5	Two beam state selection in a 3D lattice. . . . .	91
8.1	Photo of vacuum chamber (side view). . . . .	94
8.2	Photo of vacuum chamber (top view). . . . .	95
8.3	Pyramid MOT operation. . . . .	96
8.4	The P-MOT and surrounding optics. . . . .	96
8.5	The anti-Helmholtz coils on the P-MOT. . . . .	97
8.6	Shim coil switching circuit. . . . .	98
8.7	3D drawing of the science chamber. . . . .	99
8.8	Circuit used to switch the S-MOT coils on and off. . . . .	100
8.9	External cavity diode laser diagram. . . . .	102
8.10	Photo of the external cavity diode laser. . . . .	104
8.11	The circuit used to lock the diode lasers. . . . .	105
8.12	Optical setup used for absorption spectroscopy. . . . .	107
8.13	Pump-probe saturated absorption spectrum for Rb. . . . .	107
8.14	Pump-probe saturated absorption spectrum for $^{85}\text{Rb}$ . . . . .	108
8.15	Optics setups for polarisation and DAVLL locking. . . . .	109
8.16	Polarisation spectroscopy error signal. . . . .	110
8.17	DAVLL error signal. . . . .	111
8.18	Beat note envelope. . . . .	112
8.19	Fourier transform of the beat note. . . . .	112
8.20	Optics layout used in laser cooling. . . . .	113
8.21	How a small detuning is obtained from two AOMs. . . . .	115
8.22	Optics around the science chamber. . . . .	116
8.23	The laser shutter driving circuit. . . . .	117
8.24	Shutter construction - speaker coil. . . . .	118
8.25	Shutter construction - hard disk. . . . .	119
8.26	The $\text{CO}_2$ laser optics. . . . .	120

---

8.27	Ray tracing through the four lens objective. . . . .	122
8.28	1951 USAF resolution test chart results. . . . .	123
8.29	Experiment control wiring diagram. . . . .	123
9.1	Image of cold atom cloud in the P-MOT. . . . .	126
9.2	Image of cold atom cloud in the S-MOT. . . . .	127
9.3	Photodiode used to collect S-MOT fluorescence. . . . .	128
9.4	Load curves for the S-MOT. . . . .	129
9.5	Fluorescence is plotted against Rb dispenser current. . . . .	130
9.6	Fluorescence is plotted against shim coil current. . . . .	130
9.7	Fluorescence is plotted against P-MOT current. . . . .	131
9.8	Atom number is plotted against S-MOT detuning. . . . .	132
9.9	Atom number is plotted against loading time. . . . .	132
9.10	Decay time of the S-MOT. . . . .	133
10.1	Trap loading strategies. . . . .	136
D.1	Atomic structure of Rubidium. . . . .	143
G.1	Fibre optic alignment. . . . .	147
G.2	Max/Min power vs. $\lambda/2$ waveplate angle. . . . .	148
G.3	Min/Max power vs. $\lambda/4$ waveplate angle. . . . .	148
H.1	Knife edge measurement of the S-MOT laser beam. . . . .	150

# List of Tables

2.1	Polarisabilities for Rb atoms. . . . .	23
2.2	Two-level model and polarisability approach contrasted. . . . .	24
5.1	The two different alternate-gradient strategies modelled. . . . .	62
6.1	Lens properties of the combined laser guide and magnetic lens. . . . .	74
6.2	Focus quality of the combined laser guide and magnetic lens. . . . .	80
6.3	Focus quality of the two alternate-gradient strategies. . . . .	85
8.1	Shutter design comparison. . . . .	117
8.2	High resolution objective lens design. . . . .	122
A.1	Abbreviations and acronyms. . . . .	138
B.1	Symbols used and their meaning. . . . .	139
C.1	Values and constants used. . . . .	142